## GCSE (9-1)

## Mathematics

J560/05: Paper 5 (Higher tier)
General Certificate of Secondary Education

Mark Scheme for June 2019

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

Annotations used in the detailed Mark Scheme.

| Annotation | Meaning |
| :---: | :---: |
| - | Correct |
| 3 | Incorrect |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working (after correct answer obtained), provided method has been completed |
| M0 | Method mark awarded 0 |
| M1 | Method mark awarded 1 |
| M2 | Method mark awarded 2 |
| ${ }^{\text {A1 }}$ | Accuracy mark awarded 1 |
| B1 | Independent mark awarded 1 |
| B2 | Independent mark awarded 2 |
| MR | Misread |
| SC | Special case |
| $\wedge$ | Omission sign |

These should be used whenever appropriate during your marking.
The M, A, B, etc annotations must be used on your scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate these scripts to show how the marks have been awarded.

## Subject-Specific Marking Instructions

1. M marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding M (method) marks. Therefore M0 A1 cannot be awarded.
B marks are independent of $\mathbf{M}$ (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage. SC marks are for special cases that are worthy of some credit.
2. Unless the answer and marks columns of the mark scheme specify $\mathbf{M}$ and $\mathbf{A}$ marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working full marks should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.
3. Where follow through (FT) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word their for clarity, eg FT $180 \times$ (their ' $37{ }^{\prime}+16$ ), or FT $300-\sqrt{ }\left(\right.$ their ${ }^{\prime} 5^{2}+7^{2 \prime}$ ). Answers to part questions which are being followed through are indicated by eg FT $3 \times$ their (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.
4. Where dependent (dep) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- figs 237, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point eg 237000, 2.37, 2.370, 0.00237 would be acceptable but 23070 or 2374 would not.
- isw means ignore subsequent working after correct answer obtained and applies as a default.
- nfww means not from wrong working.
- oe means or equivalent.
- rot means rounded or truncated.
- seen means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- soi means seen or implied.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (ie isw) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.
7. In questions with a final answer line following working space,
(i) if the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation $\checkmark$ next to the correct answer.
(ii) if the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation $\checkmark$ next to the correct answer.
(iii) if the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation $x$ next to the wrong answer.
8. In questions with a final answer line:
(i) If one answer is provided on the answer line, mark the method that leads to that answer.
(ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
(iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
(i) If a single response is provided, mark as usual.
(ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for A and B marks. Deduct 1 mark from any A or B marks earned and record this by using the MR annotation. M marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75 , which is seen in the working. The candidate then rounds or truncates this to $15.8,15$ or 16 on the answer line. Allow full marks for the 15.75 .
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  | $8 \times 10^{7}$ final answer | 2 | M1 for ans figs 8 or for ans $k \times 10^{7}$ where $0<k<10$ |  |
| 2 | (a) | $6 a^{11}$ | 3 | B2 for answer ka ${ }^{11}$ <br> or $\frac{6 a^{13}}{a^{2}}$ or $6 \times a^{6} \times a^{5}$ or $6 \times a^{8} \times a^{3}$ <br> shown in working OR <br> B1 for answer $6 a^{k}$ or $k a^{13}$ <br> or for $3 a^{8} \times 2 a^{3}$ or $3 a^{6} \times 2 a^{5}$ shown in working |  |
|  | (b) | $2.5 \text { or } 2 \frac{1}{2} \text { or } \frac{5}{2}$ | 3 | M1 for correct first step e.g. $6 x-10=5$ <br> M1 for $6 x=5+10$ FT their first step or for FT their $a x=b$ to $x=\frac{b}{a}$ | Do not accept $\frac{15}{6}$ as final answer but allow to imply M1M1 Embedded answer scores M2 max where $\frac{b}{a}$ is a simplified fraction (improper or mixed number) or an integer e.g. M1 for $6 x=1$ leading to $x=\frac{1}{6}$ |
| 3 | (a) | 40 | 3 | M2 for $\frac{1.68-1.20}{1.20}[\times 100]$ oe Or M1 for $\frac{1.68}{1.20}$ oe or for $1.68-1.20$ oe | $\text { eg } \frac{48}{1.20} \text { or } \frac{48}{120} \text { or } 0.4$ <br> For M1 accept 168-120 oe eg 48 M1 implied by 1.4 or 140 |
|  | (b) | 450 | 3 | M2 for $360 \div 0.8$ oe or $\mathbf{B 1}$ for $0.8[0]$ oe seen <br> or for 360 associated with $80 \%$ isw | For B1 0.8 oe seen allow fraction but not just for 80\% |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | (a) | 7 | 3 | B2 for 6.5 or $6 \frac{1}{2}$ oe or M1 for $\frac{\text { their }(106-80)}{4}$ oe | For M1 accept attempted repeated subtraction from 106 to 80 or from 26 to 0 or repeated addition of 4 from 80 to 106 or from 0 to 26 condone 1 error At least 4 correct additions or subtractions needed soi FT one error |
|  | (b) | Fewer days oe | 1 |  | e.g. smaller, less, days would be shorter, would decrease, ignore reference to numbers of days if lower |
| 5 | (a) | Four points correctly plotted | 2 | B1 for 2 or 3 correct plots | Mark in 70\% zoom, use overlay, points inside or touching circles |
|  | (b) | Negative <br> Strong | $1$ <br> 1 |  | Do not accept description of relationship <br> Accept moderate, medium etc, but not weak |
|  | (c) | Point at (4, 3.4) indicated only | 1 |  |  |
|  | (d) | Ruled line of best fit and answer FT their line $\pm 100$ | 2 | B1 for ruled line of best fit or for answer FT their line with negative gradient | Use overlay for LOBF, ruled line should be as long as the zone and should not cross the longer sides of the zone <br> Not for e.g. 6.4 thousand |


| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (e) |  | Only have data on cars up to 12 years old oe <br> or <br> Equation of line of best fit would give a negative value or zero oe | 1 |  | e.g. the trend may not continue It would give a negative cost Outside range of data provided oe The price would be below zero The price would be zero oe <br> See AG <br> Do not accept 16 is not on the graph The graph does not go to 16 <br> Ignore incorrect statements |
| 6 | (a) |  | $\frac{3}{7}, \frac{3}{7}, \frac{4}{7}, \frac{3}{7}$ correctly placed | 2 | M1 for 2 or 3 probabilities correctly placed | Accept equivalent fractions, decimals or \%s (3 figures needed for dec or \%) |
|  | (b) |  | $\frac{16}{49}$ oe | 2 | M1 for $\frac{4}{7} \times \frac{4}{7} \mathbf{o e}$ | isw cancelling/conversion to other forms |



| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 8 |  | 10 | 5 | B4 for $\frac{120}{11}$ oe or for $\frac{110}{30}$ oe and $\frac{121}{30} \mathbf{o e}$ or B3 for $\frac{110}{30}$ oe or $\frac{121}{30}$ oe OR <br> B2 for $\frac{11}{30}$ oe <br> or M1 for $\frac{1}{6}+\frac{1}{5}$ <br> or for $\frac{5}{30}$ and $\frac{6}{30}$ seen <br> M1 for $4 \div$ their $\left(\frac{1}{6}+\frac{1}{5}\right) \mathbf{o e}$ | For B4 accept 10.9... or 3.66 to 3.67 and 4.03... <br> For B3 accept 3.66 to 3.67 or 4.03... <br> 0.366 to 0.367 or $36.6 \%$ to $36.7 \%$ <br> For M1 intention to add the fractions eg use of 0.16 to $0.17+0.2$ oe percentages <br> e.g. $4 \div(0.16$ to $0.17+0.2)$ oe <br> NB can score B2 M1 or M1M1 |
| 9 | (a) | 1:5 | 2 | B1 for [1] $k$ : $5 k$ with both values numeric | e.g. B1 for 0.2 : 1, 30: 150 |
|  | (b) | $\begin{array}{r} 30,75,75 \\ \text { and } 30,30,120 \end{array}$ | 4 | B3 for 30, 75, 75 or 30, 30, 120 or B2 for $p=30$ or M1 for $180 \div(1+5)$ FT their (a) If 0 scored, SC2 for $150,15,15$ | Accept each set in any order Could be on diagram |
| 10 | (a) | $0.1 \dot{6}$ final answer | 2 | B1 for 0.16.... | Accept unambiguous alternate notation for the recurring decimal e.g. B1 for $0.166,0.168,0.16$ |



| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) | -5 | 5 | M3 for $2(3 x-2+7)=4 x$ oe or $\frac{2 x-7+2}{3}=x$ oe or M2 for $2(3 x-2+7)$ oe seen or $\frac{2 x-7+2}{3}$ oe seen <br> or M1 for $3 x-2$ or $3 x+5$ oe seen or $2 x-7$ or $2 x-5$ oe seen <br> M1dep for correct rearrangement of their eqn with at least 2 terms in $x$ to $a x+b=0$ or better | For method marks, condone inclusion of multiplication signs <br> Method must be seen in working space for part (b) <br> If brackets omitted then allow recovery for method <br> For M3 eg $2 x-7=3 x-2$ <br> M1dep on at least M1 earned previously e.g. $2(3 x-2)+7[=4 x]$ scores M1 and then can earn M1 dep if they then correctly rearrange to $a x=b$ |
| 13 |  | It should be a curve with increasing gradient oe <br> It should go through $(0,1)$ | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ |  | Accept alternate forms e.g. correct sketch <br> See AG Incorrect statements treat as choice. Incomplete statements ignore |




| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 16 | (a) | [Angle DCB =] 180-112 <br> [Opposite angles in a] cyclic quadrilateral [are supplementary] oe <br> [Angle BCO =] 68-33 $=35$ $y=35 \text { and }$ <br> [triangle BOC =] isosceles with no incorrect statement | M1 <br> M1 <br> M1 <br> M1 | Must show the subtraction <br> Must show the subtraction | Must not be associated with wrong angle <br> Do not accept any incorrect statement e.g. opposite angles in a cyclic quad are equal, angles of a cyclic quad $=180$. <br> Condone issues with spelling provided clear <br> Must not be associated with wrong angle If [angle $B C O=$ ] 180-112-33 is shown this implies first M1 and third M1 <br> For M1 must mention isosceles with $y=35$ stated not just shown on the diagram |
| 16 | (b) | 55 <br> Angles in triangle [BOC sum to 180] oe <br> Angle at circumference is half angle at centre oe | B1 <br> M1 <br> M1 | Accept [triangle $\mathrm{BOC}=$ ] isosceles | Accept triangle and 180 without 'angle’ <br> Must use correct terminology, angle, circumference, half oe (or double oe), centre. Accept arc for circumference If more than 2 reasons given then treat each extra reason as choice |
| 17 | (a) | $(x+4)^{2}-13$ final answer | 3 | B1 for $(x+4)^{2}$ <br> B2FT for [ + ] 3 - their $(\mathrm{a})^{2}$ after $(x+\text { their } a)^{2}$ correctly evaluated or B1 for [+] 3 - their $a^{2}$ shown <br> If 0 scored, $\mathbf{S C 2}$ for final answer $(x+4)-13$ | FT can be implied eg $(x+2)^{2}-1$ gets B2FT |




| Question |  | Answer | Marks | Part marks and guidance |  |  |
| :--- | :--- | :--- | :--- | :---: | :--- | :--- |
| $\mathbf{1 9}$ | (a) |  | 1.7 cao | $\mathbf{1}$ |  | Mark at most accurate <br> i.e. do not allow $1.65=1.7$ |
|  | (b) | (i) | $[a=]-5$ <br> $[b=] 4$ | $\mathbf{2}$ | B1 for each or for $-5 x+4$ seen |  |
|  |  | (ii) | Correct line ruled on grid | $\mathbf{M 2}$ | Strict FT $y=$ their ax + their $b$ <br> M1 for correct $y$-intercept (FT their $b)$ or <br> correct gradient (FT their a) or for freehand or <br> broken 'correct' line FT $y=$ their $a x+$ their $b$ <br> or for at least 3 correct plots and no incorrect <br> plots FT $y=$ their ax + their $b$ | For M2 line must cross curve <br> For M2 or M1, accuracy $\pm 1$ small square at <br> provided it fits on the grid) and gradient $\pm 1$ <br> small square vertically for a run of 1 unit <br> horizontally <br> Do not follow through if $a=0$ and/or $b=0$ |

## APPENDIX

Exemplar responses for Q5e

|  | Response | Mark |
| :--- | :--- | :--- |
| $\mathbf{1}$ | The line of best fit would hit zero before 16 years old and a car is always worth something | $\mathbf{1}$ |
| $\mathbf{2}$ | 16 years is off the scale so the estimate would be inaccurate as the correlation may change <br> (lgnore insufficient first part - this gets it for the final part underlined) | $\mathbf{1}$ |
| $\mathbf{3}$ | No data for a car 16 years old | $\mathbf{1}$ |
| $\mathbf{4}$ | The equation will give a negative value | $\mathbf{1}$ |
| $\mathbf{5}$ | Data is only provided for cars up to 12 years old, so we don't know beyond that | $\mathbf{1}$ |
| $\mathbf{6}$ | Should not extrapolate beyond 12 years | $\mathbf{1}$ |
| $\mathbf{7}$ | Car prices will never be zero BOD | $\mathbf{1}$ |
| $\mathbf{8}$ | Rate of value loss may not be constant $\quad$ (BOD trend does not continue) | $\mathbf{1}$ |
| $\mathbf{9}$ | 16 years is not on the graph | $\mathbf{0}$ |
| $\mathbf{1 0}$ | Worth is not decreasing at a standard rate, it is fluctuating | $\mathbf{0}$ |
| $\mathbf{1 1}$ | Graph only goes to 12 years and it is less likely cars will be 16 years old | $\mathbf{0}$ |
| $\mathbf{1 2}$ | Starts to curve off which is not shown on the graph | $\mathbf{0}$ |
| $\mathbf{1 3}$ | Just an average, depends on the condition, mileage etc | $\mathbf{0}$ |
| $\mathbf{1 4}$ | Extrapolated | $\mathbf{0}$ |
| $\mathbf{1 5}$ | Line of best fit won't reach | $\mathbf{0}$ |

Exemplar responses for Q13

|  | Response | Mark |
| :---: | :---: | :---: |
| 1 | It should be a curve It should start at 1 not 0 | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ |
| 2 | It should start at 1 on the $y$-axis It should be an exponential curve | $\begin{aligned} & 1 \\ & 0 \end{aligned}$ |
| 3 | Correct sketch shown of curve passing through 1 on $y$-axis | 2 |
| 4 | It should not start at 0 It should curve up | $\begin{aligned} & 0 \\ & 1 \end{aligned}$ |
| 5 | $5^{\wedge} 0=1$ not 0 so $y$-values should increase by 1 Line should curve sharply upward | $\begin{aligned} & \hline 1 \\ & 1 \end{aligned}$ |
| 6 | Put numbers on axes Make gradient steeper | $\begin{aligned} & \hline 0 \\ & 0 \end{aligned}$ |
| 7 | Graph should be steeper not directly proportional | 0 |
| 8 | As increases, y increases even more <br> The graph should start above 0 and $5^{0}=1 \quad$ BOD above implies starts at $y=1$ on $y$ axis | $\begin{aligned} & \hline 0 \\ & 1 \end{aligned}$ |

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